



ANCHORED PILES IN DEEP EXCAVATIONS: A CASE STUDY

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Abstract

Traditionally the temporary support of deep excavations in gravelly soils consists of non-secant piles anchored at multiple levels. The standard practice for its design is the use of simplified methods and limit equilibrium principles, such as Terzagui's method or the FHWA 99 guidelines, despite the fact that these procedures were originally developed for sheet piles or anchored walls on relatively shallow excavations supporting a medium dense soil. The present study draws on the applicability of such simplified tools to model the static response of deep excavations in stiff gravelly soils and their implications for the design. For that purpose, the static response of an excavation supported with anchored piles was evaluated with a detailed finite element model of a case study and the results compared with the simplified hand-calculation procedures. The study unit was the excavation for the Beauchef Poniente building located in the fluvial deposits of the Mapocho River in Santiago, which has a 6200 m² plan area and a depth of 28 m. The excavation was supported with reinforced concrete piles of 1 m in diameter and anchored at three levels. A plain strain finite element model was developed in PLAXIS 2D using the Hardening Soil constitutive relation to capture the shear-deformation response of the gravel. The soil parameters were calibrated against large scale triaxial tests on Santiago gravel and the displacement profiles measured with inclinometers. The analysis showed that the static earth pressures on the pile and anchors tension computed from the 2-D non-linear finite elements model are in excellent agreement with the simplified design procedures such FHWA guidelines or simple elastic beam approximations.

Keywords: deep excavation, soldier piles, earth pressures, anchors, numerical modeling



1. Introduction

The depth of underground levels in buildings has increased significantly in recent years due to the greater demand for space in high-density urban areas. In Chile, at the beginning of the nineties, underground levels in Santiago reached depths of 10 to 13 m [1]. Currently, these depths are being exceeded; such is the case of the Costanera Center Building, with five underground levels to a depth of 20 m, the Titanium La Portada tower, with seven underground levels to a depth of 25 m, and the Territoria 3000 building, with nine underground levels to a depth of 32 m. The latter is the deepest excavation performed to date in Santiago.

To optimize the use of space, these underground levels use the entire building plan area. Their construction requires vertical cuts in the ground and a temporary retaining system. In dense soils without a water table, such as in Santiago gravels, the most widely used construction method is reinforced concrete (RC) soldier pile walls [2,3] anchored at one or more levels. During the different construction stages, it is necessary to know the pile deformations and stress state of the soil to evaluate the global stability of the excavation. Accordingly, the pile performance can be assessed based on ground displacement measurements or indirectly through numerical models. Similarly, the stress state within the ground can be evaluated through a numerical analysis or in an approximate manner using simplified models based on limit equilibrium, and by re-analyzing historical cases. However, there are not enough empirical data to validate the use of these simplified methods in dense gravel, such as in Santiago soils or in excavations of depths greater than 10 m.

Therefore, the objectives of this research are (i) to develop and calibrate a finite element model for a deep excavation in Santiago gravels and (ii) to compare the magnitude and distribution of earth pressures transferred to the piles obtained from the numerical model and based on simplified methods.

2. Background

The magnitude and distribution of earth pressures in retaining structures vary significantly by construction method and excavation sequence. In particular, during the construction of soldier pile walls anchored at one or more levels, the excavation sequence and installation and stressing of the anchors induce load and deformation patterns in the walls that cannot be correctly approximated by means of traditional limit equilibrium methods [4, 5] used to design cantilever walls.

The FHWA-IF-99-015 report 'Ground Anchors and Anchored Systems' [3], presents a study that describes the excavation sequence and behavior of earth pressures on a short wall anchored at two levels with a dry, medium sand. In the first stage, the soil is excavated past the first line of anchors, such that the wall cantilevers and earth pressures approximate the active condition. Then, the upper anchors are then stressed, and the earth pressure increases significantly, exceeding the passive state around the anchors in some cases. In the following stage, the excavation continues, creating a pressure bulb around the anchor and a redistribution of stresses towards the upper anchors and bottom of the excavation. Similar effects occur with the lower anchor stress and the last stage of the excavation, which results in a pressure distribution that peaks at the anchor level and is lower between the anchors and towards the ends of the wall, as indicated in Figure 1.

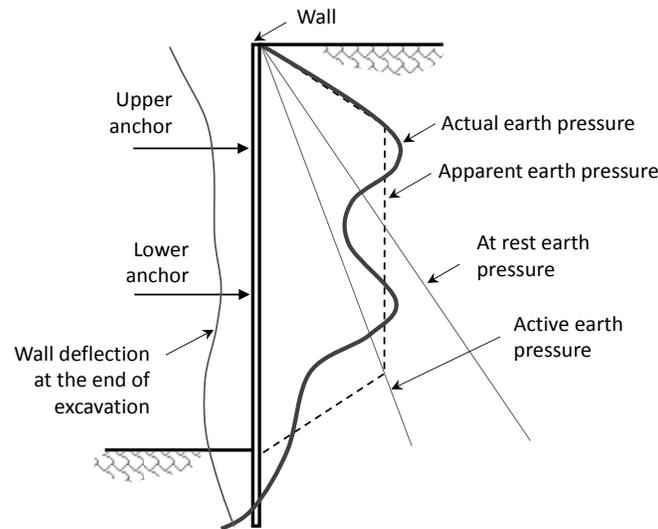


Figure 1. Earth pressures and wall deflection in anchored walls, modified from [3]

In the static design of anchored piles, it is common to represent the actual earth pressure distribution through an apparent trapezoidal or uniform earth pressure diagram. The first recommendations to evaluate design pressures were proposed by Terzaghi and Peck [6], based on load measurements in the struts of an internally braced excavations. In these recommendations, homogeneous soils and plane strain conditions are assumed. It is also assumed that the walls deform enough to mobilize the full shear strength of the soil. In addition, sands are assumed to behave drained, and clays are assumed to behave in undrained conditions. Following the seminal work by Terzaghi and Peck, much research has been conducted on the subject [3,7,8,9].

Load transfer between soldier piles and the ground is controlled by the “arching effect”, which consists of the redistribution of soil stresses due to the local displacement of the ground between stationary points [10]. Detailed study of the interaction between soil and piles have been developed through a 3-D numerical analysis [12,13], which takes into account the rotation of principal stresses between piles. Likewise, Hashash and Whittle [14] modeled the arching effect in deep excavations with clay, and the calculated earth pressure values were consistent with in-situ measurements; however, the model in the study was limited to unanchored walls. The construction sequence and dynamic response of anchored piles in a 12 m deep excavation in Santiago gravel have been studied thoroughly [15]. Through the numerical analysis, the authors evaluated the redistribution of stresses resulting from the construction sequence and calibrated an equivalent plane strain model to study the dynamic response of the problem, which significantly reduced the calculation time.

The instrumentation for the Beauchef Poniente Building, included inclinometers to measure the deformations in a pile [16]. The study was followed by a numerical model of the construction sequence in FLAC2D [17] using an elastoplastic model.

Design recommendations for anchored soldier pile walls are based one of the following strategies [1]. In the first case, the pile is analyzed as a stiff element with an active earth pressure distribution, whereas in the second case, the pile is modeled as a continuous beam with a uniform earth pressure distribution. In the Chilean design code for excavation supports [18], the static design of elements with a single anchor level considers the most unfavorable case between uniform and triangular earth pressure distributions and, in the seismic case, considers an inverted triangular distribution. Similarly, for elements with multiple supports, static and seismic designs are performed with a uniform pressure. These methods produce conservative estimations of stress in the anchors, particularly in the seismic case, since recent studies have shown that the inverted triangular pressure distribution is an experimental outcome rather than an empirical observation [19].

In summary, previous studies focused on shallow earth retaining systems, such as anchored walls or piles, particularly in soft or low-density soils, which are susceptible to large displacements. The existing literature on

anchored piles in deep excavations with dense soils, such as the gravels found in the Santiago valley, is scarce, and the applicability of traditional methods requires further analysis.

3. Case study

The Beauchef Poniente Building, which is located in Santiago (33.458°S – 70.664°W), is a seven-story reinforced concrete structure with six underground levels and a depth of 28 m. The underground levels have an area of 6 200 m², and their construction was achieved using a temporary excavation system supported by 114 1-m diameter soldier piles spaced at 2.95 m center-to-center and anchored at three levels. The piles are made of H30 concrete ($f_c' = 25$ MPa) and have a longitudinal reinforcement area of 81.43 cm² and transverse reinforcement with an area of 2.01 cm² spaced at 10 cm. The nominal bending strength ($M_n = 1\,236$ kN·m) and shear strength ($V_n = 1\,360$ kN) of the pile were estimated based on guidelines in ACI318-14 [20]. The excavation plan view and details of the studied pile are shown in Figure 2.

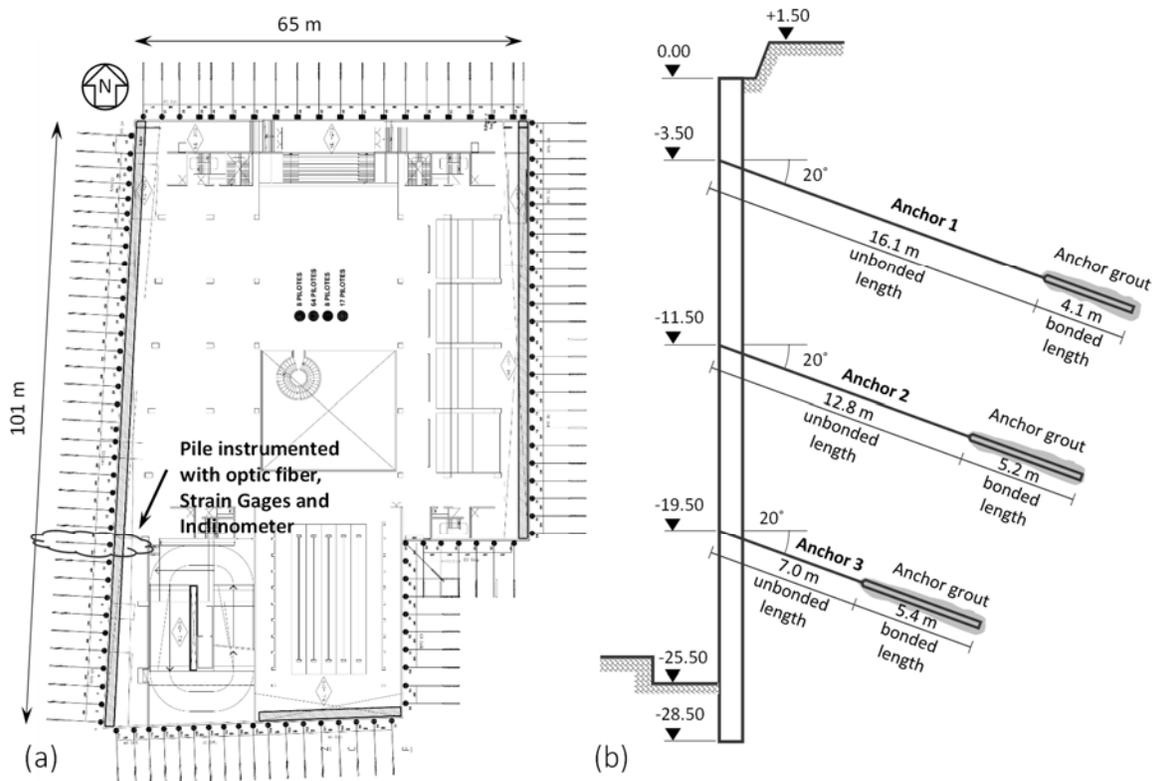


Figure 2. (a) Plan view of the Beauchef Poniente Building and (b) elevation of the studied pile

The soils present at the site are fluvial sediments known as ‘Santiago gravel’. These gravels form two distinct units known as the first and second Mapocho deposits, with average thicknesses of 22 m and 6 m, respectively. The first and deepest deposit is a dense sandy gravel ($\gamma = 23$ kN/m³, $\phi = 53^\circ$, $c = 24$ kN/m²) with a natural water content of 4% - 6%. On top of this gravel is the second and younger deposit, which corresponds to a dense gravel with low plasticity silts ($\gamma = 22.5$ kN/m³, $\phi = 45 - 53^\circ$, $c = 20$ kN/m²). The water table is below 50 m. For a detailed description of the geotechnical parameters of Santiago gravel, refer to [21-22].

Excavation sequence can be broadly described in eight stages, which encompass the construction of the pile, progress on the excavation, and installation and stressing of the anchors, as shown in Table 1.



Table 1 – Construction sequence

Excavation Depth		Stage description
Stage 1	0.0 m	Pile drilling and construction, L=28.5 m
Stage 2	-4.5 m	Excavation of 4.5 m
Stage 3	-4.5 m	First line of anchors at z=-3.5 m, pre-stress load 1004 kN
Stage 4	-12.5 m	Excavation of 8.0 m
Stage 5	-12.5 m	Second line of anchors at z=-11.5 m, pre-stress load 1297 kN
Stage 6	-20.5 m	Excavation of 8.0 m
Stage 7	-20.5 m	Third line of anchors at z=-19.5 m, pre-stress load 1331 kN
Stage 8	-26.0 m	Excavation of 5.5 m, end of excavation

The inclinometer data used in this research was corrected to eliminate the bias-shift error using standard reduction techniques [20]. The pile was instrumented with a digital MEM inclinometer system and readings were taken every 1.0 m starting at depth of 27m. The inclinometer, manufactured by RST, uses bi-axial MEMs to measure inclination on two orthogonal directions, say A and B. Once measures are taken along the positive directions, the probe is rotated 180 degrees to measure inclination along the negative directions A- and B-. These MEMs produce an output signal that is proportional to the sine of the inclination plus a bias or error. The term ‘bias shift’ of inclinometer readings refers to a systematic error due to a drift of the sensor bias, such that the algebraic sum of the readings on opposite directions or ‘checksum’ is twice the bias. This bias is initially set to zero at the factory, but its value drifts over time due to aging and instrument wear among other factors, all of which were properly accounted for.

4. Numerical model

A finite element model of the excavation was developed to evaluate the distribution of the static earth pressures, the internal forces on the piles and stress in the anchors. The simulation was performed in PLAXIS 2D and included the site stratigraphy, a typical pile on the western side of the excavation, and three anchor levels according to the geometric specifications of the project, as shown in Figure 3. The model was discretized using finite elements with 15 nodes and a maximum size of 2.4 m on the edges and 0.6 m in the anchor zone. The boundary nodes on the vertical edges were restrained horizontally, whereas the nodes on the model base were restrained vertically. The pile was modeled using 2D beam elements of rectangular cross section with a moment of inertia equivalent to a set of circular piles spaced at 2.95 m center-to-center; the three anchors lines were modeled as cable elements with bonded and unbonded segments, and pre-stress loads of $T_{01}=1004$ kN, $T_{02}=1297$ kN, and $T_{03}=1331$ kN for the top, middle and bottom anchor, respectively. The interaction between the soil and the pile was modeled with PLAXIS’s interface element, consisting of two sets of elastic perfectly plastic springs. The construction sequence was implemented according to the stages indicated in Table 1, which assumed drained conditions for the soil.

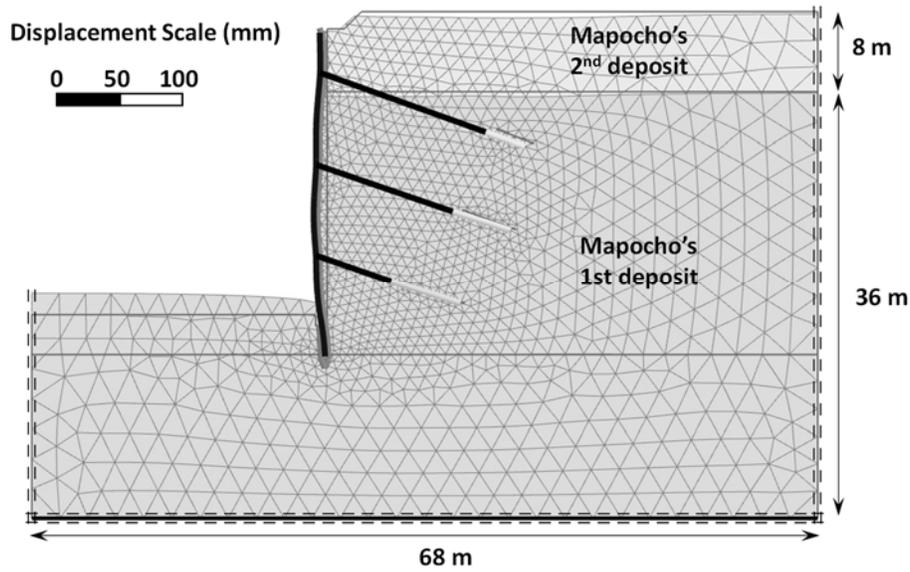


Figure 3. Deformed finite element mesh at the end of Stage 8

Given that the excavation did not experience large deformations ($\Delta/H < 0.001$), the Hardening Soil constitutive relationship [21] was used to capture the stiffness and non-linearity in the range of small deformations. The shear stiffness and shear strength parameters of the gravels are shown in Table 2; these parameters were determined based on the stress-strain response measured in isotropically consolidated drained triaxial tests for confining stresses of 22 kPa, 43 kPa, 60 kPa and 81 kPa [22]. As seen in Figure 4, the simulated stress strain response of the soil is in good agreement with the measured response. No volumetric response data was available from this set of experiments.

Table 2 – Soil Parameters based on the measured triaxial response (initial values)

Parameter	1 st deposit	2 nd deposit
E_{50}^{ref}	136 MPa	45.5 MPa
E_{oed}^{ref}	110 MPa	36.4 MPa
E_{ur}^{ref}	409 MPa	137 MPa
c_{ref}	22.6 kPa	12.3 kPa
m	0.5	0.5
ϕ_p	53.3°	53.3°
Ψ	23.3°	23.3°
v_{ur}	0.2	0.2
R_f	0.9	0.9
$K_{0,NC}$	0.33	0.33

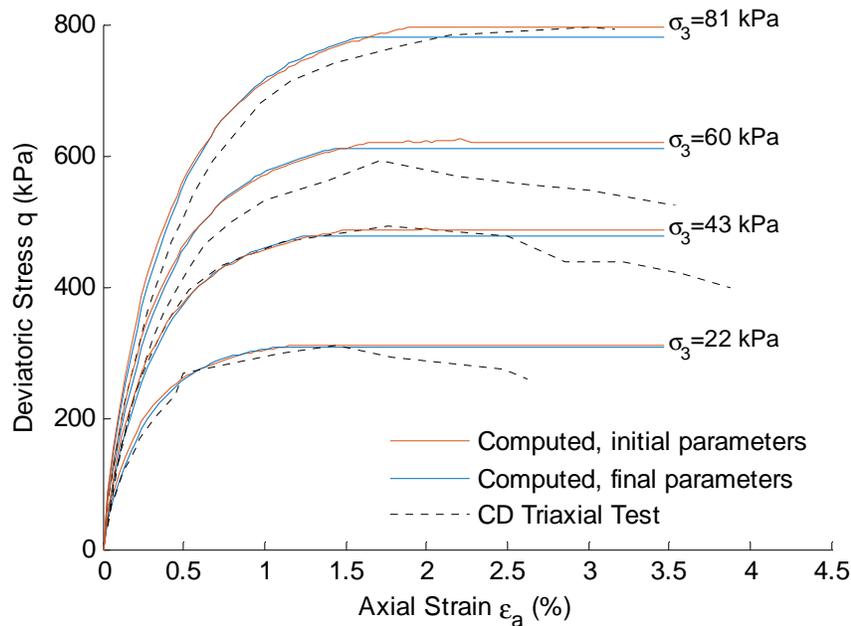


Figure 4. Comparison between measured and simulated stress-strain response in triaxial compression tests using the ‘initial’ and ‘final’ set of model parameters

To match the pile displacements measured in situ [16], the model parameters of the soils described above were further adjusted by increasing the reference Young modulus and Oedometric modulus of the 1st gravel deposit by approximately 17%. In both gravel deposits the at-rest coefficient of earth pressure was decreased by 24%. The critical state friction angle and dilatancy angle were only slightly decreased. The final set of model parameters is presented in Table 3 and the shear strain response is also shown in Figure 4; the final set of parameters was used throughout the study in all stages of construction. The resulting displacement profiles are shown in Figure 5 for different stages. Note that selected model parameters enable a good representation of the wall displacement in stages four through six, however, some differences are apparent in the final stage.

Table 3 – Soil Parameters based on the measured wall deflection (final values)

Parameter	1 st deposit	2 nd deposit	Difference with respect to initial values	
E_{50}^{ref}	160 MPa	45.5 MPa	+17 %	-
E_{oed}^{ref}	128 MPa	36.4 MPa	+16 %	-
E_{ur}^{ref}	480 MPa	137 MPa	+17 %	-
c_{ref}	22.6 kPa	12.3 kPa	-	-
M	0.5	0.5	-	-
ϕ_p	53°	53°	<1%	<1%
Ψ	23°	23°	<2%	<2%
ν_{ur}	0.2	0.2	-	-
R_f	0.9	0.9	-	-
$K_{0,NC}$	0.25	0.25	-24 %	-24 %

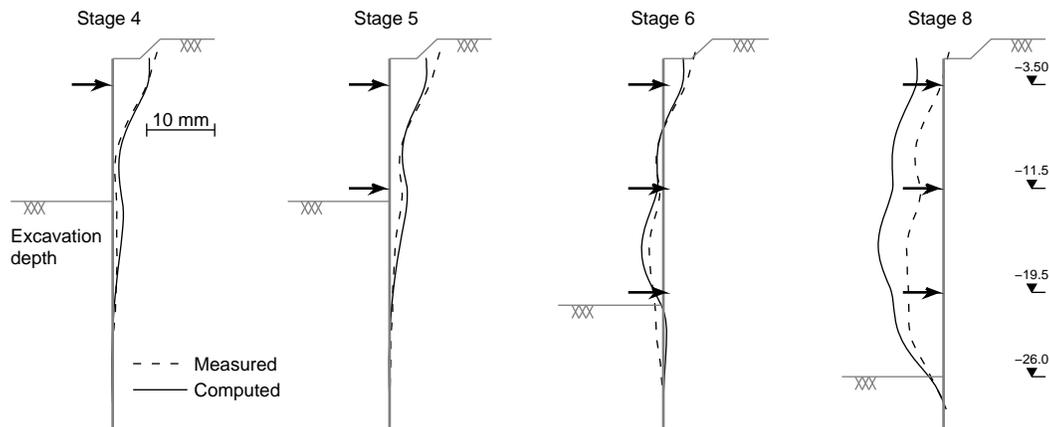


Figure 5. Comparison between measured and computed pile displacements

5. Analysis of results

The lateral earth pressure on the piles computed with the finite element model are shown in Figure 6 at the end of stages 2, 4, and 8. These stages represent different boundary conditions in the pile, which correspond to the pile in cantilever, the pile with one anchor level, and the pile with three anchor levels, respectively. For reference, this figure includes the apparent pressure diagram recommended by the FHWA guidelines for anchored piles [3], and an earth pressure range limited by the active Coulomb condition ($K_A=0.11$) and the at-rest conditions ($K_0=0.20$) computed for a friction angle of 53° .

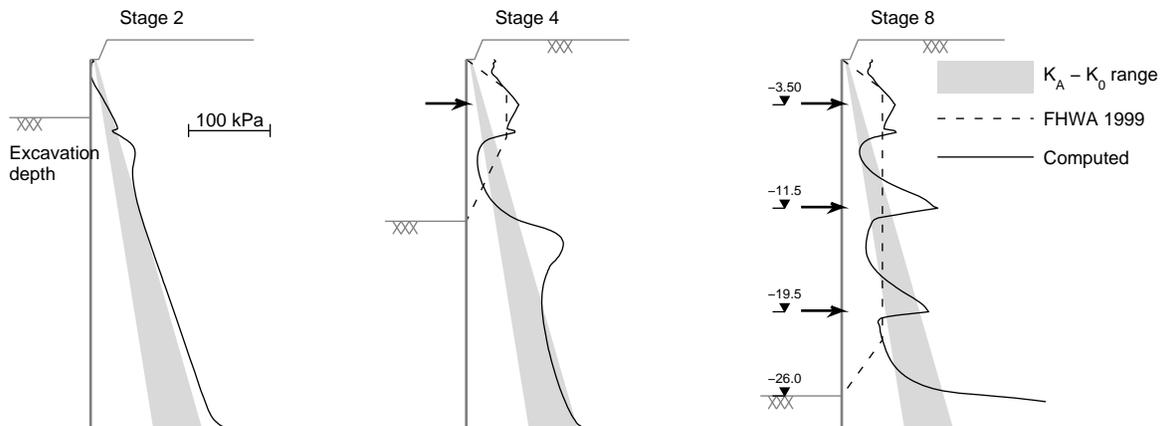


Figure 6. Diagrams of computed and apparent earth pressures on the pile

At the end of stage 2, a reduction in the lateral earth pressure on the cantilever pile and a slight increase in pressures just below the dredge line are apparent. At greater depths, there are no significant disturbances on the pile, and therefore, pressures remain near K_0 conditions. After stressing the first anchor and excavating down to an elevation of -12.5 m (stage 4), the resulting lateral earth pressures adequately fits the trapezoidal distribution proposed by FHWA for a 12.5m pile, and the pile deflection beneath the dredge line induces a significant increase in soil pressures. Towards the bottom of the pile, one can see a slight reduction in horizontal pressures as a result of vertical unloading.

In the last stage, the pressures obtained from the finite element model are concentrated at the anchor levels, which are greater than the initial at-rest earth pressures. Between anchors, the soil pressure is reduced to a value that approximates the Coulomb active condition, whereas at the bottom of the excavation, the rotation in the pile generates increased pressures due to passive soil resistance.

Although the apparent pressure distribution proposed by the FHWA does not adequately represent the shape of computed pressures at the final stage, it provides an adequate stress level for designing the pile and anchors for the entire history of the excavation. To evaluate the internal forces in the pile in accordance with the apparent pressure distribution defined by the FHWA, a simplified model of the pile was implemented. It consists of a frame element fixed at the dredge line and lateral supports that represent the anchors, as shown in Figure 7(a). The moment of inertia was defined as $I=0.0491 \text{ m}^4$, the young modulus as $E=24 \text{ GPa}$ and the trapezoidal pressure diagram with maximum ordinate $p=50 \text{ kN/m}$ as per FHWA specifications. Figure 7(b) shows that the simplified model of the pile correctly reproduces the shear stresses and bending moments obtained from the finite element model. This result validates the use of the trapezoidal-shaped lateral earth pressures in deep excavations with dense gravels, such as Santiago gravels.

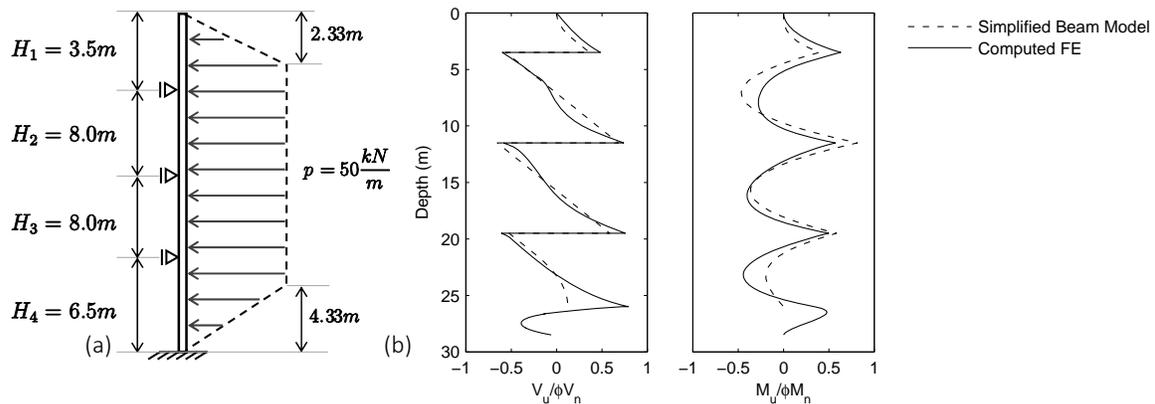


Figure 7. (a) Simplified frame model for evaluation of internal forces on the pile, (b) Normalized shear and normalized bending moments on the pile

Finally, at the end of the construction sequence the load at the three anchor calculated with the finite element model are $T_1 = 1100 \text{ kN}$, $T_2 = 1350 \text{ kN}$, and $T_3 = 1400 \text{ kN}$ for the top, middle and bottom anchor, respectively. These values are slightly higher than the loads obtained with the FHWA recommendations based on tributary areas with differences that do not exceed 10%.

6. Discussion

The study of deep excavations in gravelly soils showed that apparent earth pressure diagrams for piles anchored at one level are in good agreement with the lateral earth pressures computed in finite element simulations. Yet, for two and three anchor levels the apparent earth pressures significantly underestimate the computed earth pressures, especially around near the anchors. The simplified FHWA approach, however, provides sufficiently accurate values of design bending moment and shear forces on the piles.

Simulating the static response of deep basement retaining gravelly soils remains troublesome, in part because the documented stress-strength and stress-strain parameters for gravels apply only for low levels of confining stress. Thus, reliable numerical models for deep excavations should be complemented at least with deformation profiles of piles as measured with inclinometers.

7. Conclusions

A finite element model was developed to simulate the static behavior of a deep excavation in the gravel of Santiago supported by soldier piles anchored at three levels. The numerical model was used to estimate the earth pressures transferred to the pile, moment and shear forces on the pile, and the anchors stresses. Furthermore, the applicability of simplified hand calculation methods on stiff gravelly soils was analyzed. From the results, the following can be concluded:

- The selection of soil parameters based on shear strength tests available for Santiago gravels is not enough to reproduce the behavior of the pile during the different construction stages. It could be argued that these



laboratory tests encompass a limited range of confining pressures. However, this is a recurring problem in geotechnical engineering, in which the predictive capacity of numerical models is at least questionable due to the great heterogeneity of the materials and the broad assumptions of typical numerical models.

- The calibration of the soil parameters with triaxial test data was complemented with displacement measurements obtained with an inclinometer data. To this effect, the Young modulus and Oedometric modulus of the 1st gravel deposit was slightly increased and the coefficient of lateral earth pressure on both deposits were slightly decreased. This final set of model parameters allowed for a good comparison of pile deformations in all the construction stages.
- For the case of the pile supported by a single level of anchors (stage 4), the apparent pressure distribution proposed by the FHWA is a good approximation to the lateral earth pressures calculated with the finite element model.
- With two or more anchor levels, the lateral earth pressures vary significantly throughout the pile and cannot be correctly approximated through a trapezoidal or uniform pressure diagram. However, the trapezoidal distribution is adequate for the design of the pile and leads to slightly conservative values of bending moment and shear forces.
- The distribution of internal stresses in the pile is reasonably well approximated using a simplified beam element model, which significantly reduce the computational times.

8. Acknowledgements

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